

LINKED QUESTIONS

Q1. Consider the finite automata of four states $M=(\{Q0,Q1,Q2,Q3\},\{0,1\},\delta,F)$ with δ given by

	<i>0</i>	<i>1</i>
<i>Q0</i>	<i>Q1</i>	<i>Q1</i>
<i>Q1</i>	<i>Q1</i>	<i>Q1</i>
<i>Q2</i>	<i>Q2</i>	<i>Q2</i>
<i>Q3</i>	<i>Q3</i>	<i>Q3</i>

Q1(a) A final state to be in F for the empty string to be accepted is

A) Q0 B) Q1 C) Q2 D) Q3

Q1(b) Another final state to be in F for $(0+1)^$ to be accepted is*

A) Q0 B) Q1 C) Q2 D) Q3

Answer Q1(a) A Q1(b) B

Q2. Consider the finite automata of four states $M=(\{Q0,Q1,Q2,Q3\},\{0,1\},\delta,F)$ with δ given by

	<i>0</i>	<i>1</i>
<i>Q0</i>	<i>Q1</i>	<i>Q1</i>
<i>Q1</i>	<i>Q0</i>	<i>Q0</i>
<i>Q2</i>	<i>Q2</i>	<i>Q2</i>
<i>Q3</i>	<i>Q3</i>	<i>Q3</i>

Q2(a) A final state to be in F for the empty string to be accepted is

A) Q0 B) Q1 C) Q2 D) Q3

Q2(b) Another final state to be in F for $((0+1)(0+1))^$ to be accepted is*

A) Q0 B) Q1 C) Q2 D) Q3

Answer Q2(a) A Q2(b) A

Q3. Consider the finite automata of four states $M = (\{Q0, Q1, Q2, Q3\}, \{0, 1\}, \delta, F)$ with δ given by

	0	1
<u>Q0</u>	<u>Q1</u>	<u>Q1</u>
<u>Q1</u>	<u>Q0</u>	<u>Q0</u>
<u>Q2</u>	<u>Q2</u>	<u>Q2</u>
<u>Q3</u>	<u>Q3</u>	<u>Q3</u>

Q3(a) A final state to be in F for the empty string to be accepted is

- A) Q0 B) Q1 C) Q2 D) Q3**

Q3(b) Another final state to be in F for $((0+1))^*$ to be accepted is

- A) Q0 B) Q1 C) Q2 D) Q3**

Answer Q3(a) A Q3(b) B

Q4. Consider the finite automata of four states $M = (\{Q0, Q1, Q2, Q3\}, \{0, 1\}, \delta, F)$ with δ given by

	0	1
<u>Q0</u>	<u>Q1</u>	<u>Q1</u>
<u>Q1</u>	<u>Q1</u>	<u>Q1</u>
<u>Q2</u>	<u>Q2</u>	<u>Q2</u>
<u>Q3</u>	<u>Q3</u>	<u>Q3</u>

Q4(a) A final state to be in F for the empty string to be accepted is

- A) Q0 B) Q1 C) Q2 D) Q3**

Q4(b) Another final state to be in F for only the empty string to be accepted is

- A) Q0 B) Q1 C) Q2 or Q1 D) Q3 or Q2**

Answer Q4(a) A Q4(b) D

Q5. Consider the grammar

$S \rightarrow aSa | bSb | b | c$

Q5(a) The rules to be added for palindromes to be accepted are

$S \rightarrow a$ and $S \rightarrow \epsilon$ B. $S \rightarrow aS$ and $S \rightarrow \epsilon$ C. no rules D. $S \rightarrow \epsilon$

Q5(b) The rules to be added further for all palindromes over $\{a,b,c\}$ to be accepted is

A. $S \rightarrow cSc$ B. $S \rightarrow acS$ C. $S \rightarrow aSc$ D. no rules required

Answer: Q5(a) A Q5(b) A

Q6. Consider the finite automata given below over the alphabet $\{0,1\}$

	0	1
Q0	Q1	Reject
Q1	Q0	Reject
Q2	Reject	Reject
Q4	Reject	Reject

Let Q0 be the start state

Q6(a) A state to be made final for the empty set to be accepted is

A) Q0 B) Q1 C) Q2 D) Q3

Q6(b) A state to be made final for the empty string to be in the set accepted is

A) Q0 B) Q1 C) Q2 D) Q3

Q6(c) A state to be made further final for the set of all even number of 0's to be accepted is

A) Q0 B) Q1 C) Q2 D) Q3

Q6(d) A state to be made further final for all the odd number of 0's to be accepted is

A)Q0 B)Q1 C)Q2 D)Q3

Q6(e) A state further to be made final for all the 0's to be accepted is

a)Q0 B)Q2 C)Q3 D) No other state

Answer:Q6(a) (A);Q6(b)(A);Q6(c)A;Q6(d)B;Q6(e)D

Q7. Consider the grammar

$A \rightarrow aAb|ab$

$B \rightarrow bCc|bc$

$A1 \rightarrow a|a A1$

$B1 \rightarrow b|b B1$

$C1 \rightarrow c|c C1$

$S \rightarrow A1|B1|C1$

Q7(A) Consider augmenting the grammar with the rules

$S \rightarrow AB1|A1 B|A B1 C1| A1 B C1$

The grammar now generates

a.all strings in $L=\{a^i b^j c^k | i \text{ not equal to } j \text{ or } j \text{ not equal to } k\}$

b.only some strings in L as given in (A)

c.none of the strings in L as given in (A)

d.none of the above

Answer: (B)

Q7(B) Consider further augmenting the grammar with the rules

$S \rightarrow BC1|A1 B C1|B1B|A1 B1 B$

The grammar now generates

a.all strings in $L=\{a^i b^j c^k | i \text{ not equal to } j \text{ or } j \text{ not equal to } k\}$

- b. only some strings in L as given in (A)*
- c. none of the strings in L as given in (A)*
- d. none of the above*

Answer(F)

Q7(C) The rule that must be added to the grammar to accept L is

- a. $S \rightarrow A1C1$*
- b. $S \rightarrow AC1$*
- c. $S \rightarrow A1B$*
- d. $S \rightarrow SS$*

Answer(A)

Q8. Consider the dfa $M = (\{Q0, Q1, Q2, Q3\}, \{0, 1\}, q0, \delta, F)$ where the state transition function is given in the table below

	<i>0</i>	<i>1</i>
<i>- $\rightarrow Q0$</i>	<i><u>Q0</u></i>	<i><u>Q1</u></i>
<i><u>Q1</u></i>	<i><u>Q2</u></i>	<i><u>Q1</u></i>
<i><u>Q2</u></i>	<i><u>Q2</u></i>	<i><u>Q2</u></i>
<i><u>Q3</u></i>	<i><u>Q3</u></i>	<i><u>Q2</u></i>

Q8(a) A state that should be in F for 0^ to be accepted by the fa is*

- A) Q0 B) Q1 C) Q2 d) Q3*

*Q8(b) A further state that should be made final for 0^*1^* to be accepted is*

- Q0 B) Q1 C) Q2 D) Q3*

Q8(c) The minimal automata after the above to modifications has

- 3 states B) 2 states C) 4 states D) 1 state*

Answer: Q8(a) A; Q8(b) B; Q8(c) A

Q9. Consider the pushdown automata

$M = (\{Q_0, Q_1, Q_f\}, \{0, 1\}, \{Z_0, X\}, Q_0, \delta, \{Q_f\})$ where δ is given by

$$\delta(Q_0, a, Z_0) = (Q_0, XZ_0)$$

$$\delta(Q_0, a, X) = (Q_0, XX)$$

$$\delta(Q_0, b, X) = (Q_1, \varepsilon)$$

$$\delta(Q_1, \varepsilon, Z_0) = (Q_f, --)$$

Q9(a) A move that must be added to M to accept $L = \{a^n b^n \mid n > 1\}$ is

A) $\delta(Q_0, b, X) = (Q_f, --)$ B) $\delta(Q_1, b, X) = (Q_1, \varepsilon)$ C)

$\delta(Q_1, b, X) = (Q_f, --)$ D) $\delta(Q_1, b, X) = (Q_0, XX)$

Answer: (B)

Q9(b) A move that must further be added to M to accept $L = \{a^m b^n \mid n \leq m, m, n > 1\}$ is

A) $\delta(Q_0, b, X) = (Q_f, --)$ B) $\delta(Q_1, \varepsilon, X) = (Q_f, \varepsilon)$ C)

$\delta(Q_1, b, X) = (Q_f, --)$ D) $\delta(Q_1, b, X) = (Q_0, XX)$

Answer: (B)

Q10. Consider the pda

$M = (\{Q_0, Q_1, Q_f\}, \{0, 1\}, \{Z_0, X\}, Q_0, \delta, \{Q_f\})$ where δ is given by

$$\delta(Q_0, 0, Z_0) = \{(Q_0, XZ_0)\}$$

$$\delta(Q_0, 1, X) = \{(Q_1, \varepsilon)\}$$

$$\delta(Q_1, 1, X) = \{(Q_1, \varepsilon)\}$$

$$\delta(Q_1, \varepsilon, Z_0) = \{(\phi, --)\}$$

Q10(a) The move that must be added to M to accept $L = \{0^n 1^n \mid n > 1\}$ is

A) $\delta(Q_0, 0, X) = \{(Q_0, XX)\}$ B) $\delta(Q_0, 0, X) = \{(Q_1, XX)\}$

C) $\delta(Q_0, 0, X) = \{(Q_0, XXX)\}$

D) None of the above

Answer: (A)

Q10(b) The move in Q10(a) must be modified to accept $L = \{0^m 1^n \mid m \leq n \leq 2m, m, n > 1\}$ by

A) $\delta(Q_0, 0, X) = \{(Q_0, XX), (Q_0, XXX)\}$

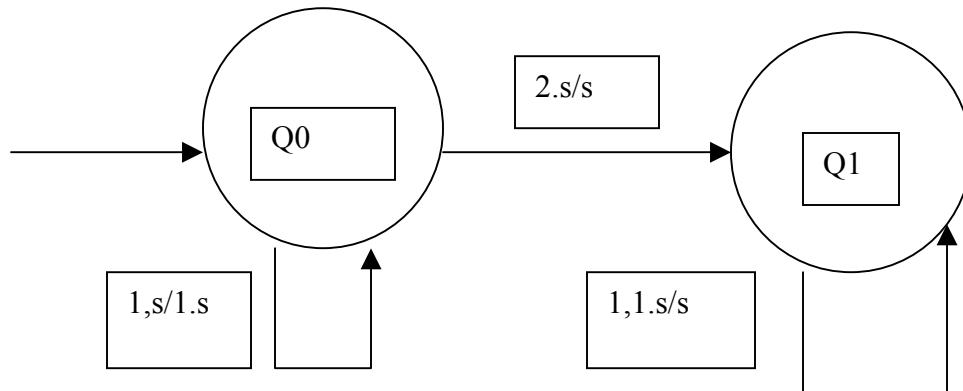
B) $\delta(Q_0, 0, X) = \{(Q_1, XX), (Q_0, XX)\}$

C) $\delta(Q_0, 0, X) = \{(Q_0, XXX), (Q_1, XX)\}$

D) None of the above

Answer: (A)

Q11. A push down automaton (pda) is given in the following extended notation of finite state diagrams



The nodes denote the states while the edges denote the moves of the pda. The edge labels are of the form $d, s/s'$ where d is the input symbol read and s, s' are the stack contents before and after the move. For example, the edge labeled $1, s/1.s$ denotes the move from state Q_0 to Q_0 in which the input symbol 1 is read and pushed to the stack.

Q11(a) An edge that should be added to the pda to accept $L = \{1^m 2 1^n \mid m \leq n \leq 2m, n, m \geq 1\}$ is

A) $\delta(Q0, 1, s/11s) = Q0$ B) $\delta(Q1, 1, s/11s) = Q1$ C)

$\delta(Q0, 1, 1.s/11s) = Q0$ D) none of the above

Answer: (A)

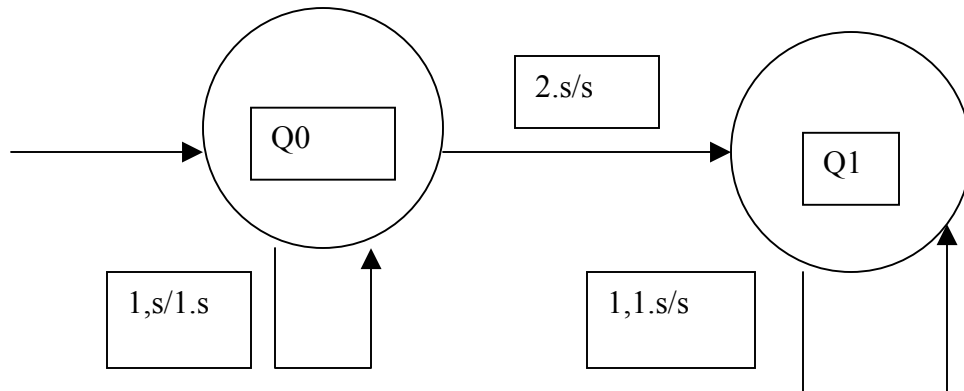
Q11(b) An edge that should further be added to the pda to accept $L = \{1^m 2 1^n \mid m \leq n \leq 2m, m, n \geq 1\}$ is

A) $\delta(Q0, 1, s/111s) = Q0$ B) $\delta(Q1, 1, s/111s) = Q1$ C)

$\delta(Q0, 1, 1.s/111s) = Q0$ D) none of the above

Answer: (A)

Q12. A push down automaton (pda) is given in the following extended notation of finite state diagrams



The nodes denote the states while the edges denote the moves of the pda. The edge labels are of the form $d.s/s'$ where d is the input symbol read and $s.s'$ are the stack

contents before and after the move. For example, the edge labeled $1,s/s$ denotes the move from state Q_0 to Q_0 in which the input symbol 1 is read and pushed to the stack.

Q12(A) The edges that should be added to the pda to accept $L = \{w^2w^R \mid w \text{ in } (0+1)^* \text{ and } w^R \text{ is the reversal of } w\}$ by empty store are

- A) $\delta(Q_0, 0, s) = Q_0$ and $\delta(Q_1, 0, 0.s/s) = Q_1$
- B) $\delta(Q_1, 0, 0.s/s) = Q_0$ and $\delta(Q_0, 0, 0.s/s) = Q_0$
- C) $\delta(Q_0, 0, s/s) = Q_1$ and $\delta(Q_1, 0, s/s) = Q_1$
- D) None of the above

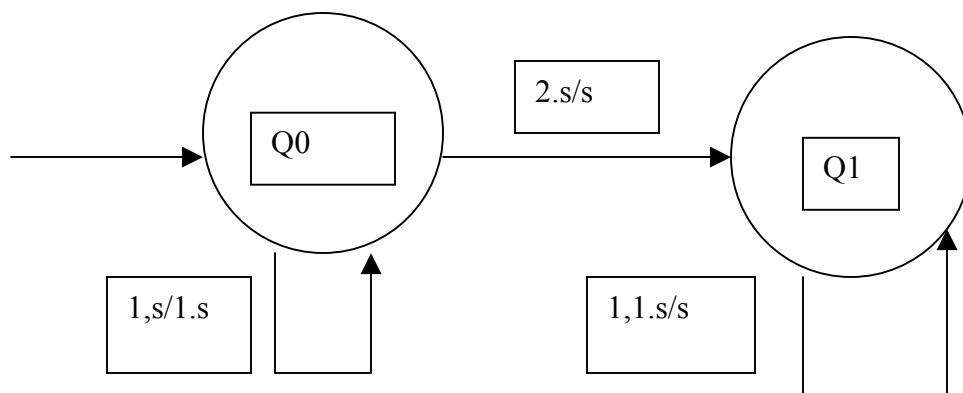
Answer (A)

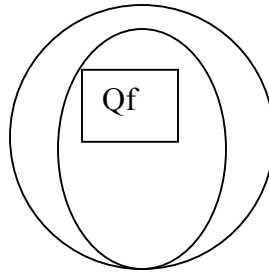
Q12(B) The edges that should further be added to the pda to accept LUL where L is given as $L = \{ww^R \mid w \text{ in } (0+1)^*\}$ by empty store are

- A) $\delta(Q_0, 1, 1.s/s) = Q_1$ and $\delta(Q_0, 0, 0.s/s) = Q_1$
- B) $\delta(Q_0, 1, 1.s/s) = Q_0$ and $\delta(Q_0, 0, 0.s/s) = Q_0$
- C) $\delta(Q_0, 1, 1.s/11.s) = Q_1$ and $\delta(Q_0, 0, 0.s/00.s) = Q_1$
- E) None of the above

Answer: (A)

Q13. A push down automaton (pda) is given in the following extended notation of finite state diagrams (Z_0 is the bottom stack marker)





The nodes denote the states while the edges denote the moves of the pda. The edge labels are of the form $d.s/s'$ where d is the input symbol read and $s.s'$ are the stack contents before and after the move. For example, the edge labeled $1,s/s$ denotes the move from state Q_0 to Q_0 in which the input symbol 1 is read and pushed to the stack.

Q13(a) Edges that should be added to the pda to accept $L = \{1^m 21^n \mid m \leq n \leq 2m, n, m \geq 1\}$ by final state are

- A) $\delta(Q_0, 1, s/11s) = Q_0$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$
 B) $\delta(Q_1, 1, s/11s) = Q_1$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$ C)
 $\delta(Q_0, 1, 1.s/11s) = Q_0$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$ D) none of the above*

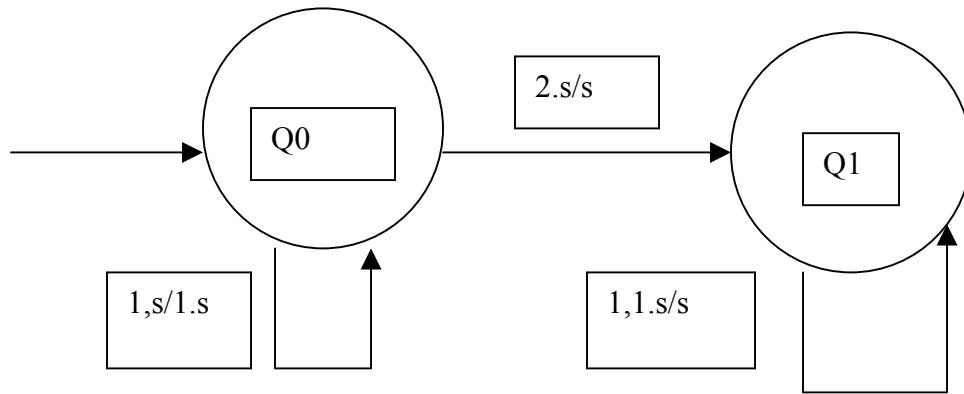
Answer: (A)

Q13(b) An edge that should further be added to the pda to accept $L = \{1^m 21^n \mid m \leq n \leq 2m, m, n \geq 1\}$ by final state are

- A) $\delta(Q_0, 1, s/111s) = Q_0$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$
 B) $\delta(Q_1, 1, s/111s) = Q_1$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$ C)
 $\delta(Q_0, 1, 1.s/111s) = Q_0$ and $\delta(Q_1, \epsilon, Z_0.s/s) = Q_f$ D) none of the above*

Answer: (A)

Q14. A push down automaton(pda) is given in the following extended notation of finite state diagrams (Z0 is the bottom stack marker)



The nodes denote the states while the edges denote the moves of the pda. The edge labels are of the form $d.s/s'$ where d is the input symbol read and $s.s'$ are the stack contents before and after the move. For example, the edge labeled $1,s/1.s$ denotes the move from state Q_0 to Q_0 in which the input symbol 1 is read and pushed to the stack.

Q14(A) The edges that should be added to the pda to accept $L=\{w^2w^R \mid w \text{ in } (0+1)^* \text{ and } w^R \text{ is the reversal of } w\}$ by final state are

F) $\delta(Q_0,0,s)=Q_0$ and $\delta(Q_1,0,0.s/s)=Q_1$ and $\delta(Q_1,\epsilon,Z_0.s/s)=Q_f$

G) $\delta(Q_1,0,0.s/s)=Q_0$ and $\delta(Q_0,0,0.s/s)=Q_0$ and $\delta(Q_1,\epsilon,Z_0.s/s)=Q_f$

H) $\delta(Q0,0,s/s)=Q1$ and $\delta(Q1,0,s/s)=Q1$ and $\delta(Q1,\epsilon,Z0.s/s)=Qf$

I) None of the above

Answer (A)

Q14(B) The edges that should further be added to the pda to accept LUL1 where L1 is given as $L1=\{wwR|w \text{ in } (0+1)^*\}$ by final state are

A) $\delta(Q0,1,1.s/s)=Q1$ and $\delta(Q0,0,0.s/s)=Q1$ and $\delta(Q1,\epsilon,Z0.s/s)=Qf$

B) $\delta(Q0,1,1.s/s)=Q0$ and $\delta(Q0,0,0.s/s)=Q0$ and $\delta(Q1,\epsilon,Z0.s/s)=Qf$

C) $\delta(Q0,1,1.s/11.s)=Q1$ and $\delta(Q0,0,0.s/00.s)=Q1$ and $\delta(Q1,\epsilon,Z0.s/s)=Qf$

J) None of the above

Answer:(A)

Q15. Consider the dfa given below

$M=\{A,B,C,D\},\{0,1\},A,\delta,\{D\}$ where δ is given the state transition table

	0	1
$\rightarrow A$	A	B
B	C	B
C	A	D
*D	A	B

Q15(A) The move that should be modified to accept $(0+1)^*101$ is

A) $\delta(D,0)=C$ B) $\delta(D,0)=D$ C) $\delta(D,0)=B$ D) None of the above

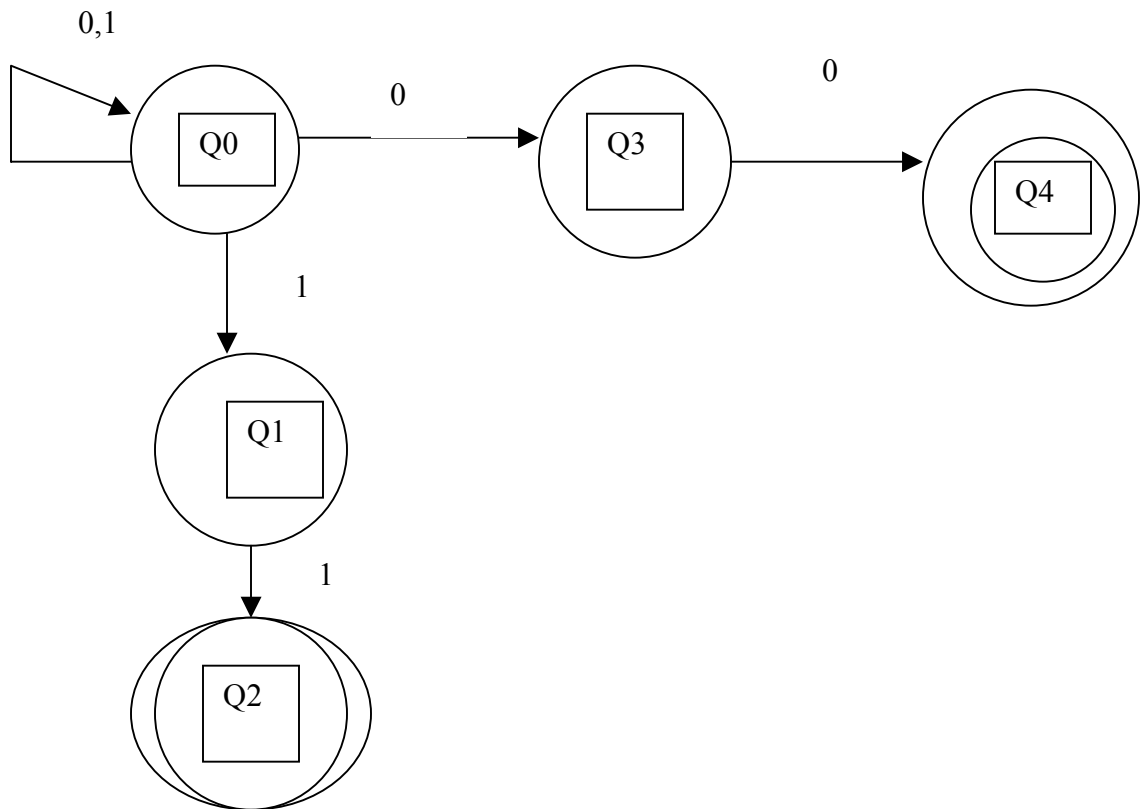
Answer: (A)

Q15(B) The minimal finite automata after the modification has

a) 3 states b) 4 states c) 2 states d) 1 state

Answer: (B)

Q16. Consider the fa given below



Q16(A) The moves that should be added to the finite automata to ensure all strings with 00 and 11 as a substring are accepted are

- a) $\delta(q_2, 0) = q_2, \delta(q_2, 1) = q_2, \delta(q_4, 0) = q_4, \delta(q_4, 1) = q_4$*
- b) $\delta(q_2, 0) = q_1, \delta(q_2, 1) = q_2, \delta(q_4, 0) = q_4, \delta(q_4, 1) = q_4$*
- c) $\delta(q_2, 0) = q_2, \delta(q_2, 1) = q_1, \delta(q_4, 0) = q_4, \delta(q_4, 1) = q_4$*
- d) $\delta(q_2, 0) = q_2, \delta(q_2, 1) = q_2, \delta(q_4, 0) = q_4, \delta(q_4, 1) = q_2$*

Answer(A)

Q16(B) The minimal finite automata after the modifications has

- a) 3 states*
- b) 4 states*
- c) 5 states*
- d) 6 states*

Answer: (C)

Q17. Ashok is given a grammar G,

$S \rightarrow aSb | ab | \epsilon$

Q17(a) He modifies the grammar with the production $S \rightarrow aS$. The resulting language L generated by the grammar is

- A) $\{a^n b^n | n > 0\}$*
- B) $\{a^m b^n | m > n, m, n > 1\}$*
- C) $\{a^m b^n | m > n, m, n > 0\}$*
- D) None of the above*

Answer: (C)

Q17(b) He further adds the production $S \rightarrow bS$

The resulting grammar generates the language L2 which is

- a) finite set*
- b) regular set*
- c) context free but not regular*
- d) empty set*

Answer: (B)

Q18. Consider the finite automata M given below

	<i>0</i>	<i>1</i>
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$\rightarrow Q_s$	R	$Q1$
R	R	R
$Q0$	$Q0$	$Q1$
$Q1$	$Q2$	$Q3$
$Q2$	$Q4$	$Q0$
$Q3$	$Q1$	$Q2$
$Q4$	$Q3$	$Q4$

Q18(A) A state to be made final to accept the set of all strings starting with a 1 that interpreted as the binary representation of an integer are congruent to 2 modulo 5 is

A)Q0 B)Q1 C)Q2 D)Q3

Answer (C)

Q18(B) A state to be further made final to accept the set of all strings starting with a 1 that interpreted as the binary representation of an integer are congruent to 2 or 3 modulo 5 is

A)Q2 B)Q3 C)Q4 D)Q1

Answer: (B)

Q18(C) A further modification is made to make all states except R final. The resulting fa accepts the set

a)1(0+1) b)(0+1)* c)0(0+1)* d) none of the above*

Answer: (A)